

## Analysis of smoke impact on clouds in Brazilian biomass burning regions: An extension of Twomey's approach

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**Abstract.** Satellite remote sensing of smoke aerosol-cloud interaction during the recent Smoke, Clouds, and Radiation–Brazil (SCAR–B) experiment is analyzed to explore the factors that determine the magnitude of the cloud response to smoke aerosol. Analysis of 2 years worth of data revealed that the response is greatest in the north of Brazil where aerosol optical depth is smallest, and tends to decrease as one moves southward, and as aerosol optical depth increases. Saturation in this response occurs at an aerosol optical depth of 0.8 in 1987 and 0.4 in 1995. To explore the reasons for this, a framework is developed in which the satellite-measured response can be compared to simple analytical models of this response and to numerical models of smoke aerosol-cloud interaction. Three types of response are identified: (1) cloud droplet concentrations increase with increasing aerosol loading, followed by saturation in the response at high concentrations; (2) as in type 1, followed by increasing droplet concentrations with further increases in aerosol loading. This increase in droplet concentration is due to the suppression of supersaturation by abundant large particles, which prevents the activation of smaller particles. This enables renewed activation of larger particles when smoke loadings exceed some threshold; (3) as in type 1, followed by a decrease in droplet number concentrations with increasing aerosol loading as intense competition for vapor evaporates the smaller droplets. The latter implies an unexpected increase in drop size with increasing smoke loading. The conditions under which each of these responses are expected to occur are discussed. It is shown that although to first-order smoke optical depth is a good proxy for aerosol indirect forcing, under some conditions the size distribution and hygroscopicity can be important factors. We find no evidence that indirect forcing depends on precipitable water vapor.

### 1. Introduction

In discussing aerosol, the term “indirect effect” has been coined to describe climatic implications for the interaction of solar radiation with aerosol particles that are hygroscopic and can participate as cloud condensation nuclei (CCN) [e.g., Twomey, 1974; Charlson *et al.*, 1992]. Twomey hypothesized that increased concentrations of atmospheric aerosol will result in higher concentrations of CCN and increased cloud droplet concentrations. This chain of events will affect cloud microphysical processes. Higher droplet concentrations will suppress drizzle formation [Albrecht, 1989] and maintain larger liquid water paths and more reflective clouds. The more reflective clouds, in theory, create a radiative forcing estimated on the global scale to range from 0.0 W m<sup>-2</sup> to -4.8 W m<sup>-2</sup> [Kaufman *et al.*, 1991; Charlson *et al.*, 1992; Kaufman and Chou, 1993; Lohmann and Feichter, 1997]. One manifestation of these processes is in “ship tracks,” the observed bright tracks in stratus clouds which are produced by the high aerosol concentrations in ship effluent [Conover, 1966; Coakley *et al.*, 1987]. Ship track experiments have been valuable in elucidating the microphysical processes that create these more reflective

clouds. (e.g., the Monterey Area Ship Track Experiment, 1994). Because the indirect effect is defined as a climatic forcing, it is necessary to evaluate it on a regional or global scale using satellite remote sensing. Such efforts have been undertaken in South American biomass burning regions by Kaufman and Nakajima [1993] and Kaufman and Fraser [1997] (hereinafter referred to as KF97), in Indonesian fires by Rosenfeld and Lensky [1998], and globally for all aerosol types collocated with marine stratus clouds by Wetzel and Stowe [1999]. These papers provide evidence in support of Twomey's theory beyond the limited environment of the ship track experiments. However, they also show variation in the strength of the indirect effect that cannot be explained by Twomey's simple formulation.

The indirect effect has also been observed by careful in situ measurements that link changes in cloud properties to changes in aerosol concentration or proxy [Leitch *et al.*, 1992; Raga and Jonas, 1993; Novakov *et al.*, 1994; Arends *et al.*, 1994; Leitch *et al.*, 1996; Reid *et al.*, 1998]. These studies identify situations where the connection between aerosol and cloud microphysics is clear, while in other situations, no connection appears to exist. However, the conclusions differ widely. For example, some in situ studies identify the indirect effect in stratiform clouds but not in cumuliform clouds [Novakov *et al.*, 1994; Reid *et al.*, 1999]. Other studies clearly find the effect in cumuliform clouds [Raga and Jonas, 1993; Arends *et al.*, 1994].

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These studies provide evidence supporting Twomey's original theory but leave us with unanswered questions. Why do we sometimes see the indirect effect and sometimes not? Is it due to variations in precipitable water vapor as hypothesized by KF97? Are the differences due to cloud type, dynamics, or turbulence, as hypothesized by *Novakov et al.* [1994], *Arends et al.* [1994], *Leitch et al.* [1996], and *Reid et al.* [1999], or can the differences be explained by variations in the aerosol properties themselves? The observational studies alone have not been able to provide definitive answers.

In this paper we turn to a combination of satellite observations and theoretical modeling for the answers to these questions. The area of interest is the biomass burning region of South America, which provided the focus of the papers of *Kaufman and Nakajima* [1993] and KF97. The primary goals of this paper are to (1) develop a framework that facilitates the intercomparison of satellite measurements and models, (2) extend the analysis of KF97 to an additional year of data and to evaluate whether the conclusions and water vapor hypothesis of the first paper are robust under different data and newer precipitable water vapor analyses, and (3) explore the reasons for the observed variability in the indirect aerosol forcing using some simple theoretical and modeling exercises.

The remainder of this paper is organized as follows: in section 2 we consider the theoretical and semiempirical theories that form the basis of evaluation of aerosol indirect forcing; in section 3 we present new analysis of the 1987 and 1995 South American biomass burning data; and in section 4 we apply the theory and modeling framework to interpret the observations. We conclude with a summary in section 5.

## 2. Simple Analytical Models

KF97 derived a measure of the aerosol indirect effect as

$$\frac{\Delta r_e}{\Delta \tau_a}, \quad (1)$$

where  $r_e$  is the droplet effective radius (the ratio of the third and second moments of the drop size distribution), and  $\tau_a$  is the smoke aerosol optical depth. To put those measurements in the perspective of prior studies, we propose the calculation of

$$\text{IE} = -\frac{\tau_a}{r_e} \frac{\Delta r_e}{\Delta \tau_a} = -\frac{d \ln r_e}{d \ln \tau_a}, \quad (2)$$

which represents the relative change in  $r_e$  for a relative change in  $\tau_a$ . IE refers to the "indirect effect" and is defined as positive in sign if an increase in  $\tau_a$  results in a decrease in  $r_e$ . The attractive feature of assessing the cloud response to aerosol using (2) is that by considering relative changes in parameters, one is less susceptible to measurement errors than in the formulation of (1). The equation for cloud optical depth  $\tau_d$  in the visible region of the spectrum is given by

$$\tau_d \approx \int_{z_b}^{z_t} \int_{r_{\min}}^{\infty} 2\pi r^2 n(r) dr dz, \quad (3)$$

where  $n(r)$  defines the drop spectrum with respect to radius  $r$ ,  $z_b$  is cloud base,  $z_t$  is cloud top,  $r_{\min}$  is the minimum drop radius, and the extinction efficiency has been assumed to be equal to 2. (A similar equation defines aerosol optical depth  $\tau_a$  but with  $n(r)$  describing the aerosol size distribution and  $z_b$

and  $z_t$ , the smoke layer boundaries; for aerosol the extinction efficiency should be explicitly calculated for the appropriate wavelength and particle composition.) For a homogeneous cloud with drop number concentration  $N_d$  and constant cloud liquid water content LWC, (3) reduces to

$$\tau_d \propto N_d^{1/3} \quad (4)$$

[*Twomey*, 1977]. Assuming that  $N_d$  obeys

$$N_d \propto N_a^{a_1}, \quad (5)$$

where  $N_a$  is the aerosol number concentration [*Twomey*, 1977], and using (4) and (5) yields

$$r_e \propto \tau_a^{-a_1/3}, \quad (6)$$

$$-\frac{d \ln r_e}{d \ln \tau_a} = \frac{a_1}{3}. \quad (7)$$

A characteristic value of  $a_1$  is 0.7 [e.g., *Pruppacher and Klett*, 1997; *Charlson et al.*, 1987], yielding IE = 0.23. Note that since  $a_1 \leq 1$ , we obtain  $0 \leq \text{IE} \leq 0.33$ .

Equation (5) is clearly a simplification of the relationship between aerosol microphysics and cloud microphysics since cloud parameters and aerosol parameters are related through the aerosol size distribution parameters and updraft velocity, rather than just through  $N_a$ .

The analysis is now extended to include aerosol size parameters. Smoke aerosol size distributions vary but are often parameterized by a lognormal function [e.g., *Remer et al.*, 1998] with respect to aerosol particle radius  $a$ :

$$n(a) = \frac{N_a}{\sqrt{2\pi} \ln \sigma a} e^{-\ln^2(a/r_g)/(2\ln^2\sigma)}, \quad (8)$$

where  $r_g$  is the median radius, and  $\sigma$  is the geometric standard deviation of the aerosol particles. We have varied  $N_a$ ,  $r_g$ , and  $\sigma$  over a broad range of parameter space to represent possible biomass burning scenarios (Table 1):

$$0.04 \mu\text{m} \leq r_g \leq 0.12 \mu\text{m}; \quad 2000 \text{ cm}^{-3} \leq N_a \leq 30000 \text{ cm}^{-3}; \quad 1.3 \leq \sigma \leq 2.2. \quad (9)$$

We assume, for the sake of simplicity, that

$$\tau_a \propto N_a^{b_1} r_g^{b_2} \sigma^{b_3}, \quad (10)$$

$$N_d \propto N_a^{a_1} r_g^{a_2} \sigma^{a_3} w^{a_4}, \quad (11)$$

where  $w$  is the updraft velocity. The first approximation is justified by the good fit to accurate calculations of  $\tau_a$  based on

**Table 1.** Lognormal Input Parameters and Updraft Velocities for the Model

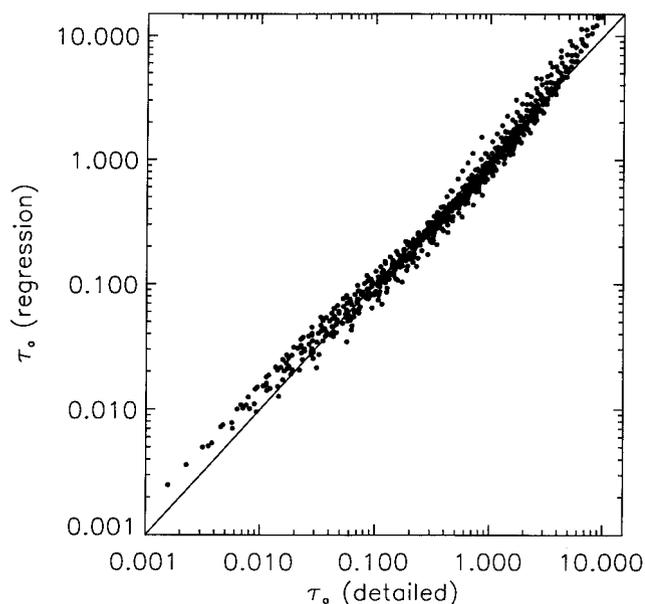
$N_a$ , $\text{cm}^{-3}$	$r_g$ , $\mu\text{m}$	$\sigma$	$w$ , $\text{cm s}^{-1}$
2000	0.04	1.3	20
4000	0.05	1.4	50
6000	0.06	1.5	75
8000	0.07	1.6	100
10000	0.08	1.7	150
12000	0.09	1.8	200
15000	0.10	2.0	300
20000	0.11	2.2	
25000	0.12		
30000			

Mie calculations for spherical aerosol particles at  $0.64 \mu\text{m}$  (Figure 1). The values of  $b_1$ ,  $b_2$ , and  $b_3$  depend on the refractive index of the aerosol (assumed here to be  $m = 1.6 + 0.1i$ ). For these conditions a least squares fit to the model output over the range of lognormal aerosol size distributions in (9) yields  $b_1 = 1.0$  (as predicted by the definition of  $\tau_a$ ),  $b_2 = 3.4$ , and  $b_3 = 5.0$ .

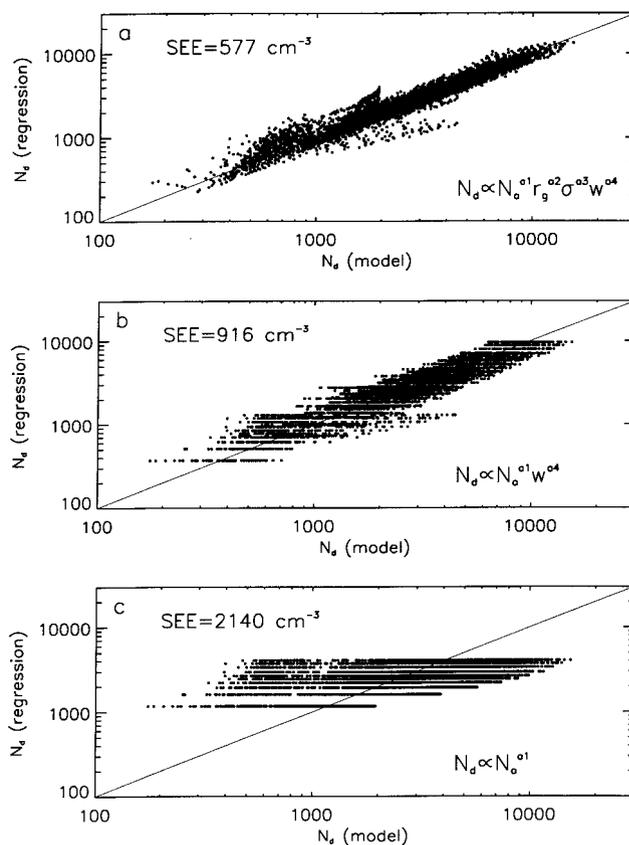
To explore the second approximation (11), we use an entraining parcel model of cloud droplet formation [Feingold and Heymsfield, 1992]. The model rigorously calculates the uptake of water vapor by a size distribution of aerosol particles, their subsequent activation, and growth by condensation. It has the flexibility to modify the solubility of the particles and the extent of entrainment drying. Entrainment is simulated as a depletion of total water mixing ratio (vapor plus liquid water) with droplets growing or evaporating in response to the change in supersaturation. It is assumed that the smoke is not replenished by entrainment since the source of the smoke is primarily a surface source.

The dynamics of the model are prescribed by a constant updraft velocity  $w$ , so it does not represent the myriad microphysical, or radiative feedbacks to the dynamics, such as destabilization/stabilization of the atmosphere as a result of absorption, or feedbacks of the aerosol to cloud liquid water path (LWP). Although the model is a simplification of real clouds, it does provide a means of exploring the relative changes in response for different aerosol input, updraft velocity, and cloud depth, and should be viewed in this light, rather than as an accurate representation of the clouds observed during SCAR-B.

The smoke particles in SCAR-B are primarily organics [e.g., Artaxo *et al.*, 1998] with rather complex water uptake proper-



**Figure 1.** Comparison of two calculations of  $\tau_a$  at  $0.64 \mu\text{m}$ . The ordinate is based on detailed extinction calculations assuming a lognormal aerosol spectrum (Table 1) comprising spherical particles, a refractive index of  $m = 1.6 + 0.1i$ , and a homogeneous smoke depth of 1 km. The abscissa values of  $\tau_a$  are based on the power law regression fit given by equation (10). The standard error of estimate for the regression fit is 0.86.



**Figure 2.** Comparison of parcel model calculations of  $N_d$  defined as all drops with  $r \geq 1 \mu\text{m}$  and  $N_d$  calculated using (a) the power law regression fit given by equation (11); (b) a two-parameter regression; and (c) a fit defined by equation (5). The results pertain to a LWP of  $15 \text{ g m}^{-2}$ , and  $\varepsilon = 0.1$ . All input parameters in Table 1 have been used to generate the regression. The standard error of estimate is indicated in each figure.

ties. They are quite different from sulfate particles in industrial regions and from the aerosol representation originally in the work of Feingold and Heymsfield [1992]. Therefore we have modified the aerosol treatment in the current work. Because no general models exist to represent the hygroscopic activity of organic particles, we have used nephelometer data collected during SCAR-B [Kotchenruther and Hobbs, 1998] as a means of constraining their water vapor uptake. The nephelometer data yield a relationship between the relative increase in the total light scattering coefficient as a function of relative humidity. The hygroscopicity of the modeled aerosol is attained by modifying the mass fraction of soluble material  $\varepsilon$  until the enhancement in scattering as a function of RH provides a reasonable fit to the observed data. Although this is a rather crude way of representing the growth properties of complex organic particles, it does provide a strong constraint on their uptake of water vapor and potential for growth into droplets.

As shown in Figure 2, (11) is a good approximation to the model output for the parameter space defined by (9) and provides a significantly better fit than more simple forms such as (5). The standard error of estimate is low, considering that  $N_d$  is typically  $10^3$  to  $10^4$ . We offer no physical justification for the power law form, other than that it provides a logical extension to the original form proposed by Twomey [1959]

**Table 2.** Coefficients  $a_n$  for  $N_d \propto N_a^{a_1} r_g^{a_2} \sigma^{a_3} w^{a_4}$ <sup>a</sup>

Aerosol Parameters/Updraft	$a_1$	$a_2$	$a_3$	$a_4$	IE
$\varepsilon = 0.1$	0.46	0.52	-0.55	0.74	0.17
$\varepsilon = 0.1$ (half adiabatic)	0.41	0.87	0.37	0.77	0.24
$\varepsilon = 0.1$ (LWP = 50)	0.44	0.48	-0.50	0.76	0.16
$\varepsilon = 1.0$	0.38	0.04	-2.80	0.52	-0.06
$0.04 \leq r_g \leq 0.08$	0.53	0.29	-0.46	0.84	0.17
$0.08 \leq r_g \leq 0.12$	0.50	-0.10	-0.51	0.73	0.12
(equivalent $\tau_a$ )	0.56	0.33	-0.43	0.79	0.19
$N_a \leq 5000 \text{ cm}^{-3}$	0.77	0.50	-0.63	0.59	0.26
(equivalent $\tau_a$ )	0.56	0.38	-0.45	0.84	0.19
$N_a > 5000 \text{ cm}^{-3}$	0.57	0.40	-0.42	0.82	0.20
$1.3 \leq \sigma \leq 1.6$	0.54	0.37	-0.35	0.87	0.19
$1.6 \leq \sigma \leq 2.2$	0.58	0.35	-0.06	0.73	0.22
$w \leq 100$	0.53	0.42	0.06	0.88	0.22
$w \geq 200$	0.59	0.31	-0.82	0.77	0.17
$w \leq 100, r_g \leq 0.08, N_a \leq 5000$	0.75	0.75	-0.33	0.77	0.30
(equivalent $\tau_a$ )	0.60	0.48	-0.31	0.83	0.22
$w \geq 200, r_g > 0.08, N_a > 5000$	0.49	-0.04	-1.13	0.84	0.08
(equivalent $\tau_a$ )	0.57	0.33	-0.41	0.79	0.19

<sup>a</sup>IE represents the indirect effect, as defined in equation (18). Coefficients are valid for LWP = 15 g m<sup>-2</sup>,  $0.04 \mu\text{m} \leq r_g \leq 0.12 \mu\text{m}$ ;  $2000 \text{ cm}^{-3} \leq N_a \leq 30,000 \text{ cm}^{-3}$ ;  $1.3 \leq \sigma \leq 2.2$ ;  $20 \text{ cm s}^{-1} \leq w \leq 300 \text{ cm s}^{-1}$ ,  $\varepsilon = 0.1$ , and an adiabatic cloud, unless otherwise stated in column 1. Equivalent  $\tau_a$  is defined as the range of  $\tau_a$  prescribed by the aerosol parameters in the row directly preceding the table entry but with no constraints on the lognormal parameters.

$$N_d \propto C^{1-k/(k+2)} w^{1.5k/(k+2)}, \quad (12)$$

where  $C$  is related to  $N_a$ , and  $k$  is a parameter related to the slope of a power law size distribution of aerosol. An advantage of (11) is that the power law form facilitates the inclusion of aerosol size parameters into the subsequent analysis. The values of  $a_1$ ,  $a_2$ ,  $a_3$ , and  $a_4$  have been derived by running the model for the input parameters indicated in Table 1, for typical meteorological conditions for the region, and performing least fit multivariate regressions to the model output. Each regression is performed on a total of 5040 realizations of the model.

The drop concentration  $N_d$  represents all drops with  $r \geq 1 \mu\text{m}$ . It is recognized that at very high  $N_a$ , many particles may exist as unactivated haze particles [e.g., Reid et al., 1999], but the exact definition of the minimum droplet radius is not very important because as soon as the larger particles that have reached their critical size begin to grow, the smaller haze particles find themselves in increasingly subsaturated conditions and evaporate rapidly, thus effectively separating haze particles from drops.

The coefficients depend on aerosol water uptake and the range of  $N_a$ ,  $r_g$ ,  $\sigma$ , and  $w$ ; the goodness of fit improves if the fit is done in piecewise fashion. Table 2 tabulates  $a_n$  for the parameter space in (9) and for a variety of conditions. Note that  $a_n$  do not vary with LWP. Discussion of the significance of these coefficients is deferred to section 4.

The analysis of smoke aerosol effect on clouds proceeds as follows:

$$\frac{dr_e}{d\tau_a} = \frac{dr_e}{dN_d} \frac{dN_d}{d\tau_a}. \quad (13)$$

At constant LWC,

$$\frac{dr_e}{dN_d} = -\frac{1}{3} \frac{r_e}{N_d}. \quad (14)$$

Then,

$$\frac{dN_d}{d\tau_a} = \frac{\partial N_d}{\partial N_a} \frac{dN_a}{d\tau_a} + \frac{\partial N_d}{\partial r_g} \frac{dr_g}{d\tau_a} + \frac{\partial N_d}{\partial \sigma} \frac{d\sigma}{d\tau_a}, \quad (15)$$

and using (10) and (11),

$$\frac{dN_d}{d\tau_a} = \frac{N_d}{\tau_a} \left[ \frac{a_1}{b_1} + \frac{a_2}{b_2} + \frac{a_3}{b_3} \right]. \quad (16)$$

Finally,

$$\frac{dr_e}{d\tau_a} = \frac{dr_e}{dN_d} \frac{dN_d}{d\tau_a} = -\frac{1}{3} \frac{r_e}{N_d} \frac{N_d}{\tau_a} \left[ \frac{a_1}{b_1} + \frac{a_2}{b_2} + \frac{a_3}{b_3} \right], \quad (17)$$

or

$$\text{IE} = -\frac{d \ln r_e}{d \ln \tau_a} = \frac{1}{3} \left[ \frac{a_1}{b_1} + \frac{a_2}{b_2} + \frac{a_3}{b_3} \right]. \quad (18)$$

Equation (18) reduces to (7) under the assumption of (5) and is thus a more general description of aerosol-cloud interaction, as defined by (2). According to (18) there are no clear bounds on the value of IE, as was the case with (7).

Because cloud reflectance and smoke optical depth are directly measured, rather than inferred, an additional parameter to explore is the relative change in cloud reflectance  $\rho$  for a relative change in  $\tau_a$ :

$$\frac{d \ln \rho}{d \ln \tau_a} = \frac{d \ln \rho}{d \ln r_e} \frac{d \ln r_e}{d \ln \tau_a}, \quad (19)$$

Using the two-stream approximation for a purely scattering cloud [Bohren, 1980],

$$\rho \approx \frac{(1-g)\tau_d}{2 + (1-g)\tau_d}, \quad (20)$$

where  $g$  is the asymmetry factor ( $\approx 0.85$ ), as well as

$$\tau_d = \frac{3 \text{ LWP}}{2 r_e} \quad (21)$$

[Stephens, 1978], we can differentiate (20) with respect to  $r_e$  to obtain

$$\frac{d \ln \rho}{d \ln r_e} = -(1 - \rho). \quad (22)$$

Then substituting (18) and (22) into (19) yields

$$\frac{d \ln \rho}{d \ln \tau_a} = \frac{(1 - \rho)}{3} \left[ \frac{a_1}{b_1} + \frac{a_2}{b_2} + \frac{a_3}{b_3} \right] = (1 - \rho) \text{IE}. \quad (23)$$

Equation (23) provides an alternative meaning of IE and an alternative means of acquiring a measure of IE from satellite retrievals. The first method, (18), represents the aerosol effect on cloud microphysics and involves retrieving  $r_e$  from mid-IR channels. The second method, (23), represents the effect of aerosol on cloud albedo and involves retrieving  $\rho$  from visible channels. These two methods are independent from a remote sensing perspective but should give the same value for IE provided the present assumptions (e.g., constant LWP) hold (see section 3.2). Additionally, differentiation of (20) with respect to  $\tau_d$  gives

$$\frac{d \ln \rho}{d \ln \tau_d} = (1 - \rho), \quad (24)$$

and dividing (23) by (24) results in

$$\frac{d \ln \tau_d}{d \ln \tau_a} = \frac{1}{3} \left[ \frac{a_1}{b_1} + \frac{a_2}{b_2} + \frac{a_3}{b_3} \right] = \text{IE}. \quad (25)$$

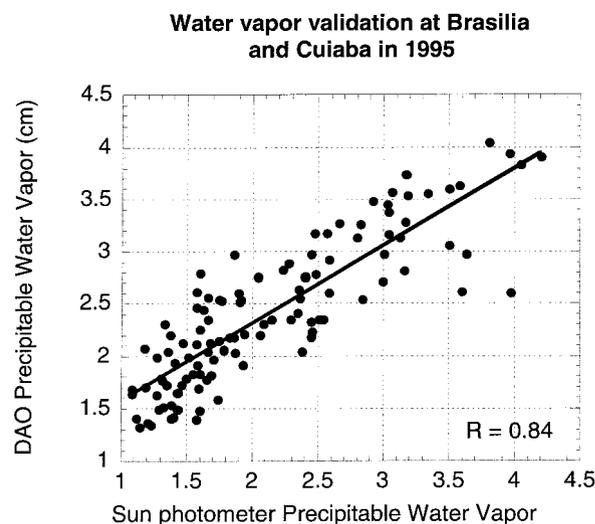
Thus (18), (23), or (25) provide a measure of the indirect effect that is based on an empirical description of aerosol-cloud interactions (equation (11)) and which can easily be tested by quantities retrieved from satellite data. Furthermore, by using (18) we can use a simple parcel model to explore theoretically the physical parameters affecting the strength of the indirect effect. The modeling effort can test the effect of parameters not readily available from satellite observations, including the size distribution and hygroscopicity of the aerosol.

### 3. Data Analysis

#### 3.1. Satellite and Water Vapor Data

The study uses AVHRR images at 1 km resolution to test the theoretical formulation of the previous section and to investigate the indirect effect in a biomass burning region. The study region over South America covers the area from  $-20^\circ\text{S}$  to  $5^\circ\text{N}$ ,  $-45^\circ\text{W}$  to  $-70^\circ\text{W}$ . Data from both the 1987 and the 1995 burning seasons (August through September) are analyzed in a consistent fashion following the methodology of Kaufman and Nakajima [1993] and KF97. AVHRR analysis yields products such as drop effective radius  $r_e$ , reflectance at  $0.64 \mu\text{m}$   $\rho$ , smoke optical depth  $\tau_a$ , and cloud top temperature  $T_c$ . Products are spatially averaged to obtain mean quantities on a  $1^\circ \times 1^\circ$  grid. Cloud fraction is also calculated for each grid square.

In addition to AVHRR data the Goddard Data Assimilation Office (DAO) provides analyzed, daily, coarse vertical resolution temperature and specific humidity profiles as well as total column precipitable water vapor PWV. The horizontal spatial resolution in 1987 is  $2.5^\circ \times 2.5^\circ$ , increasing in 1995 to  $1^\circ \times 1^\circ$



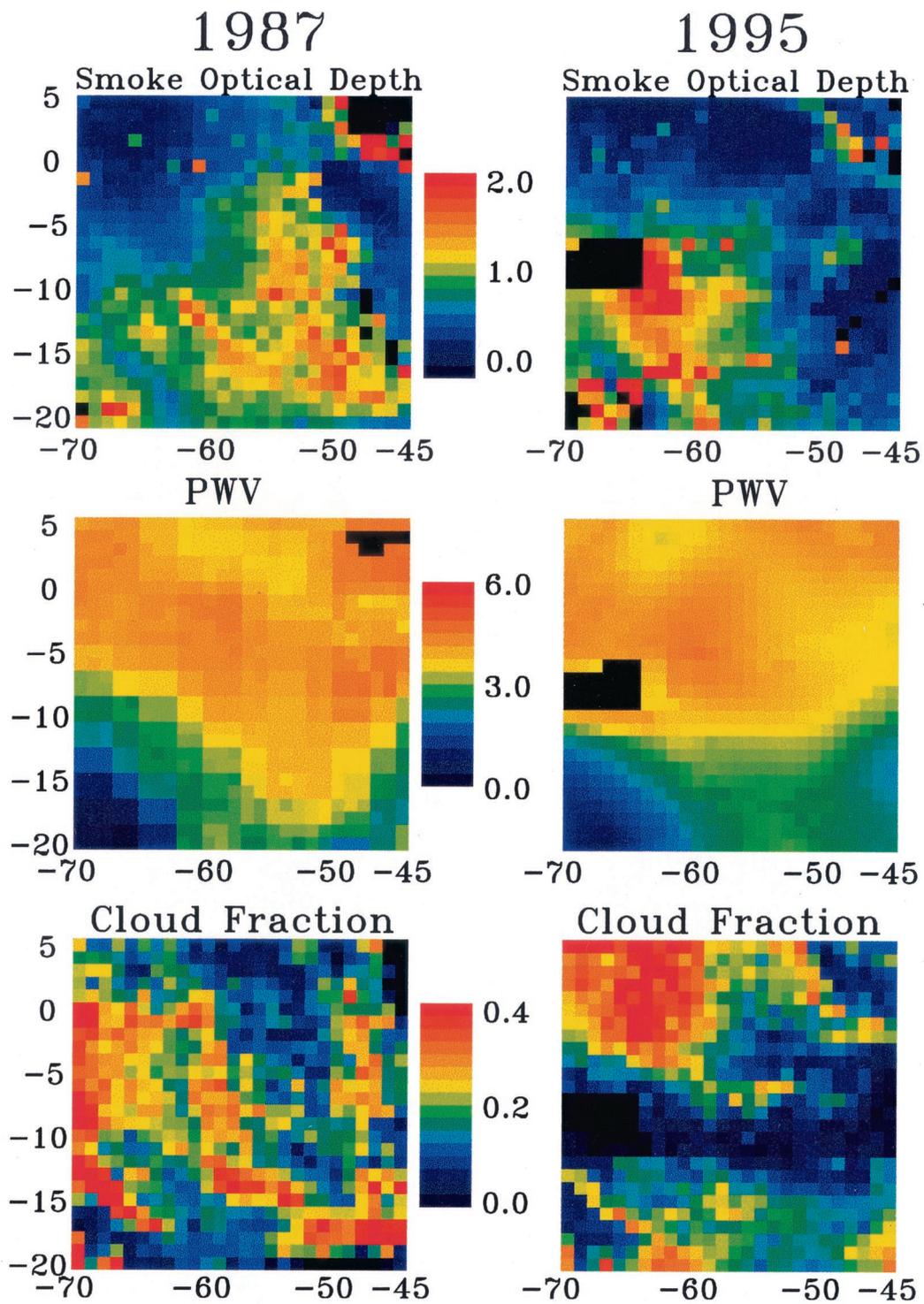
**Figure 3.** Comparison of PWV data derived from Sun photometers and DAO-derived PWV at Cuiaba and Brasilia. The correlation coefficient is 0.84.

over the entire region. Following KF97, a water vapor correction in the  $3.75 \mu\text{m}$  channel was introduced above cloud to improve the accuracy of the retrieved cloud droplet radii. However, in this study the water vapor column above the cloud level is determined from the DAO data. Previously, it was based on monthly mean values of radiosonde stations in the region with the majority of the stations occurring in the south, leaving a paucity of data in the north. To evaluate the DAO water vapor data, the values of PWV were compared with data from Sun photometers at two Aerosol Robotic Network (AERONET) stations in the region of interest [Holben *et al.*, 1998]. The Sun photometers provide hourly and daily averaged values of PWV. In Figure 3, PWV data from the Sun photometers in Cuiaba ( $16^\circ\text{S}$ ,  $56^\circ\text{W}$ ) and Brasilia ( $16^\circ\text{S}$ ,  $48^\circ\text{W}$ ) are compared to DAO PWV data. A correlation coefficient of 0.84 gives reasonable confidence in the DAO PWV data. The finer horizontal and temporal resolution of the DAO data are a significant improvement over the monthly mean data used by KF97, both in terms of water vapor correction above the clouds and in characterizing the total PWV of the column.

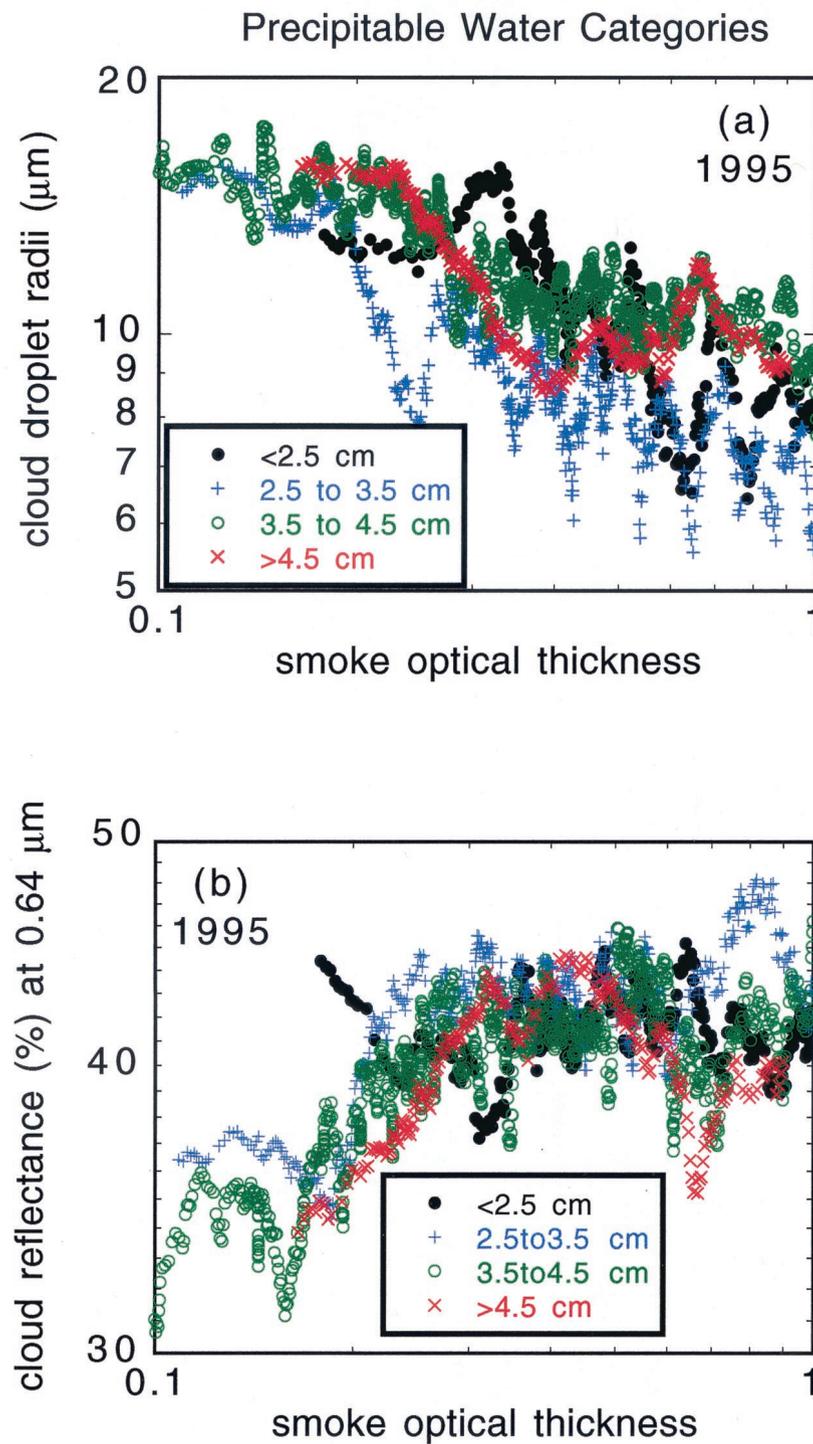
Plate 1 shows the seasonal means of some of the variables derived from daily AVHRR images and DAO water vapor. The PWV is obtained from the DAO on a coarser resolution grid in 1987. From Plate 1 we see a north-south gradient in water vapor in both years but different spatial patterns in the distribution of smoke and clouds. In 1987 the smoke also followed a north-south gradient, but in 1995, the smoke gradient is more east-west, although the far north is comparatively clean in both years. The cloud fraction distribution also shows an interannual variability. These year-to-year changes are attributed to changes in cultural burning practices as well as variability in the average circulation patterns over the region.

#### 3.2. Testing the Link Between Data Analysis and Modeling

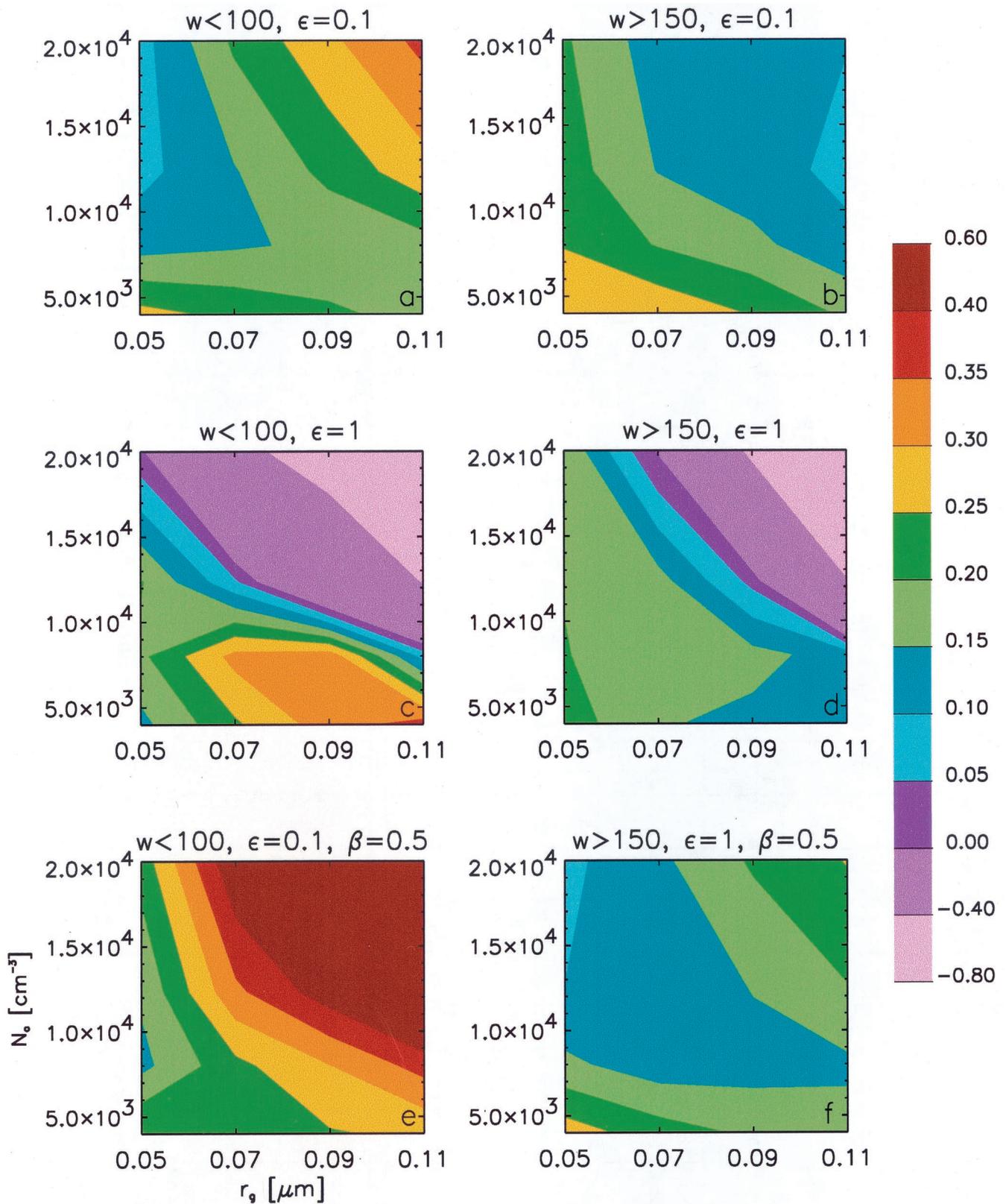
The daily  $1^\circ \times 1^\circ$  data are aggregated and sorted according to smoke optical thickness. Cloud properties are included for all clouds within the broad temperature range of 270–290 K. Figure 4 shows  $r_e$  versus  $\tau_a$  and  $\rho$  versus  $\tau_a$  over the entire region for the 1995 data set. Increases in  $\tau_a$  translate to significant decreases in  $r_e$ , and increases in  $\rho$  for  $\tau_a < 0.4$ , but



**Plate 1.** Seasonal mean values of  $\tau_a$ , PWV, and cloud fraction based on daily AVHRR images and DAO water vapor.



**Plate 2.** (a) Drop radius  $r_e$  and (b) cloud reflectance  $\rho$  at  $0.64 \mu\text{m}$  as a function of  $\tau_a$  for the different PWV zones and for 1995.



**Plate 3.** Contour plots of IE in  $N_a$ ,  $r_g$  space where the regression (equation (11)) has been applied for limited ranges of  $N_a$  and  $r_g$ ;  $w$  is vertical velocity;  $\epsilon$  is a measure of the amount of soluble material in the particles; and  $\beta$  is a measure of how close to adiabatic the clouds are.

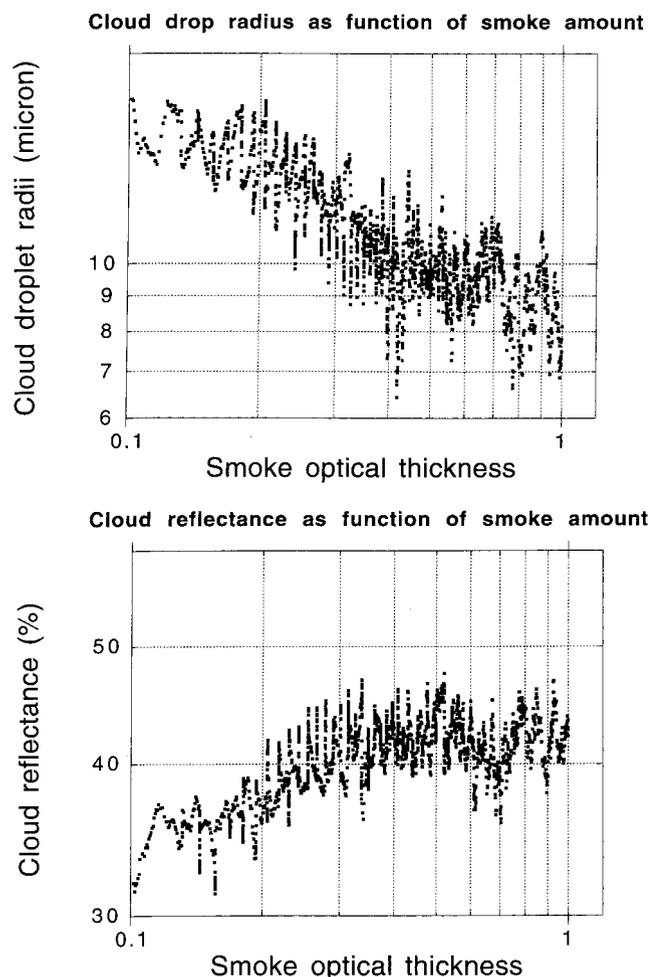
thereafter, the change is negligible. In the KF97 analysis of the 1987 data a similar relationship between the cloud variables,  $r_e$  and  $\rho$ , and smoke  $\tau_a$  is found, but the saturation in signal tended to occur at a higher  $\tau_a = 0.8$ .

A least squares linear fit is applied to the sorted data of Figure 4 in the range of  $0.10 < \tau_a < 1.00$ . The slope of this linear fit is a measure of the strength of the indirect effect corresponding to (1) for the  $r_e$  versus  $\tau_a$  relationship. Multiplying the slope by  $\tau_a/r_e$  puts the measurement in the form of (2) and eliminates systematic biases introduced by either the aerosol or the cloud retrieval algorithms. Furthermore, the normalized slope derived from the AVHRR data analysis corresponds directly to the modeling variable IE of (2) or (18). A similar analysis applied to the  $\rho$  versus  $\tau_a$  relationship corresponds directly to (23). Thus we have a link between the modeling formulation and the AVHRR data analysis.

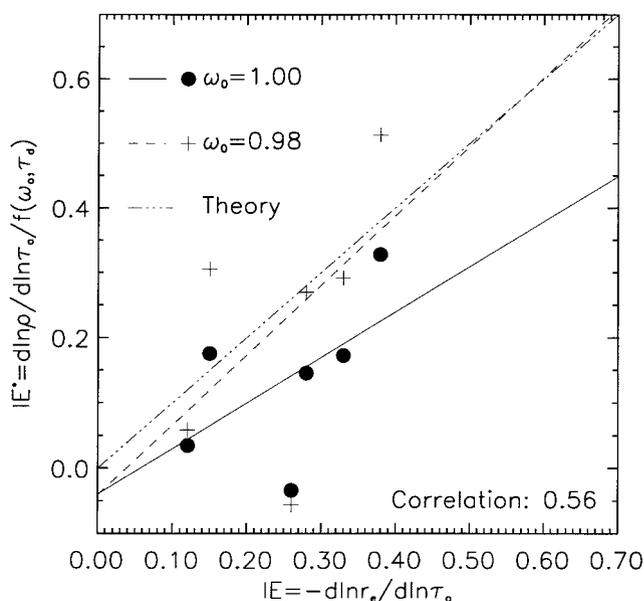
We test this link by calculating IE from the data using the two independent methods presented by either (18) or (23),

$$IE^* = \frac{1}{(1-\rho)} \frac{d \ln \rho}{d \ln \tau_a}. \quad (26)$$

In each year, 1987 and 1995, the data are divided into three latitudinal bins based on combinations of climatic variables. The north has high PWV and little smoke. The middle section



**Figure 4.** This shows  $r_e$  versus  $\tau_a$  and  $\rho$  versus  $\tau_a$  over the entire region for the 1995 data set. Note the saturation in  $r_e$  and  $\rho$  at large  $\tau_a$ .



**Figure 5.** Indirect effect (IE) as calculated using equation (18) based on  $r_e$  retrieval in the mid-IR channels, and an independent calculation of IE ( $IE^*$ ) based on equation (23) which retrieves  $\rho$  from visible channels. The circles and solid line (best fit to the data) are for the purely scattering case (equation (23)), whereas the pluses and dashed line are for the solution when  $\omega_0 = 0.98$ . Theory predicts a 1:1 relationship between the two parameters. Note that an absorbing component brings the slope of the best fit line closer to theory.

is high in both smoke and PWV, while the south is dry and smoky. Each year, in each latitude bin, the data are sorted according to  $\tau_a$ , a linear fit is applied to the proper range of data, and IE and  $IE^*$  are calculated. The relationship between the two independent calculations of IE is shown in Figure 5. The mean values for each year and latitude zone are given in Table 3. There is a relationship between the independent calculations with a correlation coefficient of 0.56. The difference between these two estimates of IE could, at least partially, be associated with feedbacks of microphysics to LWP which are not considered in the current work. Excluding the outlying point at negative  $IE^*$  improves the correlation to 0.78. Best fit lines to the data points are drawn for the purely scattering case (equation (23)) as well as for a case for which the cloud single-scattering albedo  $\omega_0 < 1$  [Stephens, 1994, page 311]:

$$\rho = \gamma_+ \gamma_- [e^{\kappa \tau_d} - e^{-\kappa \tau_d}] / \Delta(\tau_d), \quad (27)$$

where

$$\gamma_{\pm} = 1 \pm (1 - \omega_0) D / \kappa,$$

$$\Delta(\tau_d) = \gamma_+^2 e^{\kappa \tau_d} - \gamma_-^2 e^{-\kappa \tau_d},$$

$$\kappa = \{(1 - \omega_0) D [(1 - \omega_0) D + 2\omega_0 b]\}^{1/2},$$

where  $D$  is the “diffuseness” of the radiation field (assumed = 2), and  $b = (1 - g)/2$ . Note that when  $\omega_0 = 0.98$ , the best fit line to the data points lies somewhat closer to the theoretically predicted 1:1 line. Because numerous assumptions have been made in arriving at this figure, it is not suggested that  $\omega_0$  can be derived from this analysis but rather that it is likely that there is an absorbing component in the aerosol. This simple test

**Table 3.** Satellite Data Sorted According to Year and Latitudinal Zone and for Cloud Top Temperature in the 270–290 K Range<sup>a</sup>

Zone	Number of Samples	$\tau_{a,\min}$	$r_{e,\min}$ , $\mu\text{m}$	$\bar{\tau}_a$	PWV, cm	CF	IE	IE*
1987								
0°–5°N	347	0.15	13	0.40	4.0	0.25	0.33	0.17
1°–10°S	509	0.22	13	0.82	4.0	0.15	0.28	0.15
11°–20°S	165	0.27	9	1.16	2.5	0.17	0.15	0.18
1995								
0°–5°N	699	0.10	18	0.31	4.0	0.21	0.38	0.33
1°–10°S	818	0.11	7	0.50	3.9	0.13	0.12	0.03
11°–20°S	626	0.14	9	0.78	2.6	0.11	0.26	–0.03

<sup>a</sup>Mean quantities represent average conditions in the latitude zone. IE and IE\* are calculated for the subset of samples (as indicated by number of samples) for which  $\tau_a < 1.0$ . The following definitions apply:  $\tau_{a,\min}$  is the minimum aerosol optical depth;  $r_{e,\min}$  is the drop effective radius at  $\tau_{a,\min}$ ;  $\bar{\tau}_a$  is the average  $\tau_a$  in the zone; PWV is the precipitable water vapor in centimeters; CF is the cloud fraction of all squares in the zone; IE is defined by equation (3); and  $\text{IE}^* = 1/(1 - \rho)d \ln \rho/d \ln \tau_a$ .

provides confidence that we have established a working framework for linking the modeling with the data analysis.

### 3.3. Testing the Dependence of the Indirect Effect on Water Vapor

The DAO data are used together with the AVHRR data to examine the hypothesis that precipitable water vapor plays a role in influencing the pattern of the indirect effect (KF97). The data were resorted according to PWV values and then divided into four categories, regardless of latitude. Table 4 gives the mean values in each PWV category, and Plate 2 shows drop radius and cloud reflectance at  $0.64 \mu\text{m}$  as a function of  $\tau_a$  for the different categories for 1995. Contrary to the analysis of KF97, there is no systematic difference in results as a function of PWV. This is confirmed by the poor correlation between IE and PWV in Tables 3 and 4.

KF97 never directly correlated the indirect effect with precipitable water vapor. They correctly identified the latitudinal dependence of the indirect effect, which appears clearly in Table 3 in both years of data, and used latitude as a proxy for water vapor. However, the limited water vapor data available to KF97 are misleading in their spatial distribution. A reanalysis of the 1987 data set, using the DAO values of PWV, shows that although the north is wet and the south is dry, the spatial gradient in between does not correlate with the strength of the indirect effect. There is a latitudinal dependence of IE in South America, but it is not necessarily directed by PWV.

### 3.4. Testing the Dependence of the Indirect Effect on Smoke Amount

The most noteworthy feature of Table 3 is the large positive value of IE = 0.38 in the 0°–5°N zone (1995) and the steady increase in mean  $\tau_a$  from North to South. There is a trend for IE to decrease with increasing  $\tau_a$  except for one data point (1°–10°S, 1995), which has a much smaller IE than other points with similar  $\tau_a$ . The question remains whether smoke characteristics alone, as represented by  $\tau_a$ , are sufficient to modulate the strength of the indirect effect. For this answer we return to the modeling analysis.

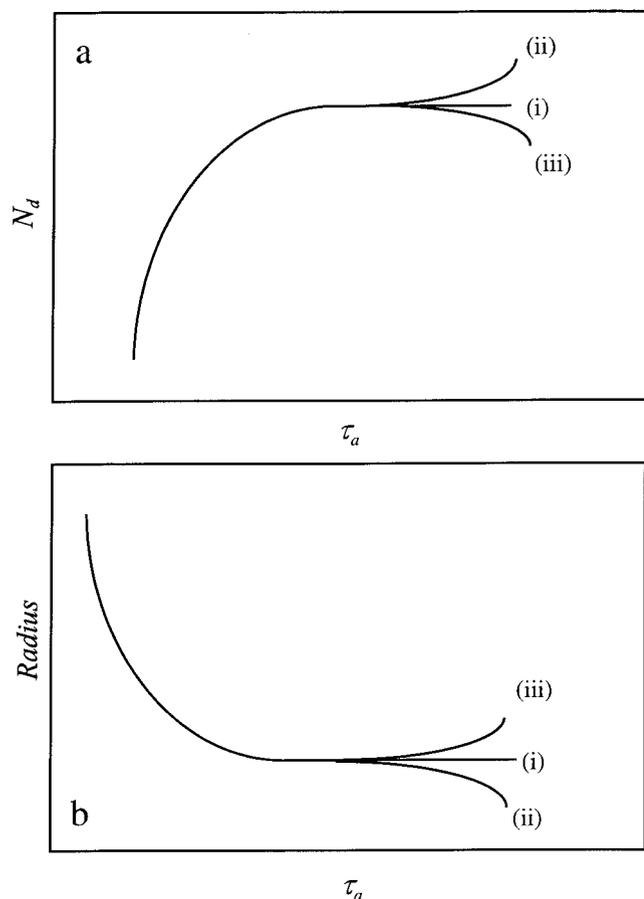
## 4. Interpretation of the Observations Using the Model

By looking to the model to interpret the data it should be stressed that the nature of the model, and its incomplete representation of natural processes, as well as the approximate form of the regressions is such that we do not intend for this analysis to be taken as quantitatively correct but rather as an indicator of the relative change in the IE for different conditions. Where there is a robust model result, we use the model to interpret the observations but recognize that other explanations could be possible. Despite these caveats, we feel it is important to make this step if we are to improve our understanding of smoke-cloud interactions.

Table 2 gives the values of  $a_n$  and IE based on (18) for

**Table 4.** Satellite Data Sorted According to Year and Precipitable Water Vapor (PWV) Bins With Analysis Consistent with Table 3

PWV, cm	Number of Samples	$\tau_{a,\min}$	$r_{e,\min}$ , $\mu\text{m}$	$\bar{\tau}_a$	IE	Latitude
1987						
<2.5	110	0.27	8	1.01	0.06	15°S
2.5–3.5	183	0.17	13	0.87	0.39	7°N
3.5–4.5	573	0.15	13	0.74	0.34	4°S
>4.5	155	0.18	13	0.70	0.34	3°N
1995						
<2.5	298	0.18	13	0.75	0.43	16°S
2.5–3.5	521	0.11	15	0.64	0.39	10°S
3.5–4.5	1101	0.10	16	0.45	0.26	2°S
>4.5	223	0.17	16	0.43	0.32	1°S

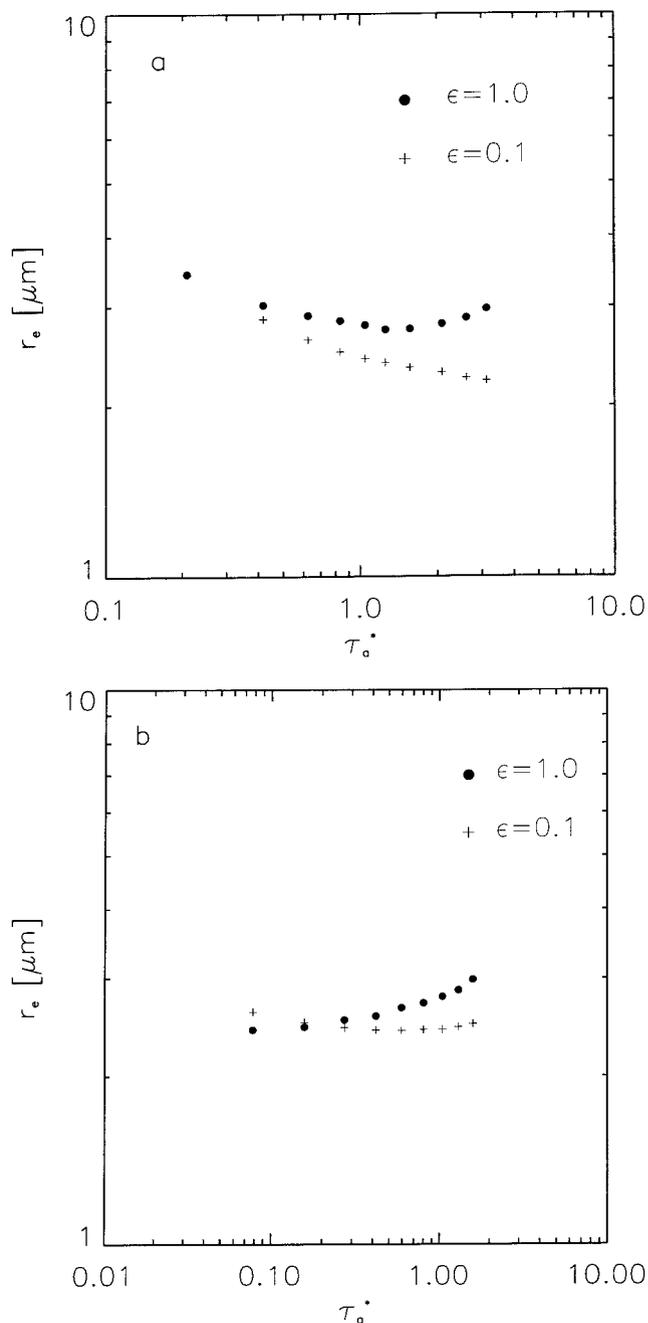


**Figure 6.** Qualitative illustration of the three identified responses of (a) drop number  $N_d$  to increasing aerosol loading and (b)  $r_e$  to increasing aerosol loading. Response *i*, saturation in  $N_d(r_e)$ ; *ii*, saturation in  $N_d(r_e)$ , followed by an increase (decrease) in  $N_d(r_e)$ ; *iii*, saturation in  $N_d(r_e)$  followed by a decrease (increase) in  $N_d(r_e)$ . All scales are linear.

different broad ranges of aerosol input parameters, as well as different dynamical forcings. We note that unlike (7), where  $0 \leq IE \leq 0.33$ , (18) yields no clear indication of the upper and lower bounds of IE because the signs of  $a_2$  and  $a_3$  are not known. Thus IE can be greater than 0.33, and under some circumstances, IE is negative (see section 4.1).

The regressions in Table 2 over a broader parameter space reveal interesting dependences of IE on  $a_n$ . For example, weak IE is primarily reflected in small or even negative values of  $a_2$  (suggesting that an increase in  $r_g$  has little effect on or even reduces  $N_d$ ), and strong negative values of  $a_3$  that imply that a broad smoke aerosol spectrum has sufficient large particles to suppress supersaturation, and therefore  $N_d$ . The latter result is analogous to that derived from Twomey's [1959] analytical equation (12) which shows that decreases in the  $k$  parameter (akin to increasing  $\sigma$ ) decrease the dependence of  $N_d$  on  $N_a$  ( $C$  in his case) and increase the dependence of  $N_d$  on  $w$ .

To supplement Table 2, Plate 3 shows contour plots of IE in  $(N_a, r_g)$  space where the regression (equation (11)) has been applied to limited ranges of  $N_a$  and  $r_g$ . By parsing the model output, one can detect trends in the coefficients and derived IE, which can be useful for interpreting observations for similar conditions. The fact that  $a_n$  change when the model output is parsed into smaller ranges of size distribution parameters is

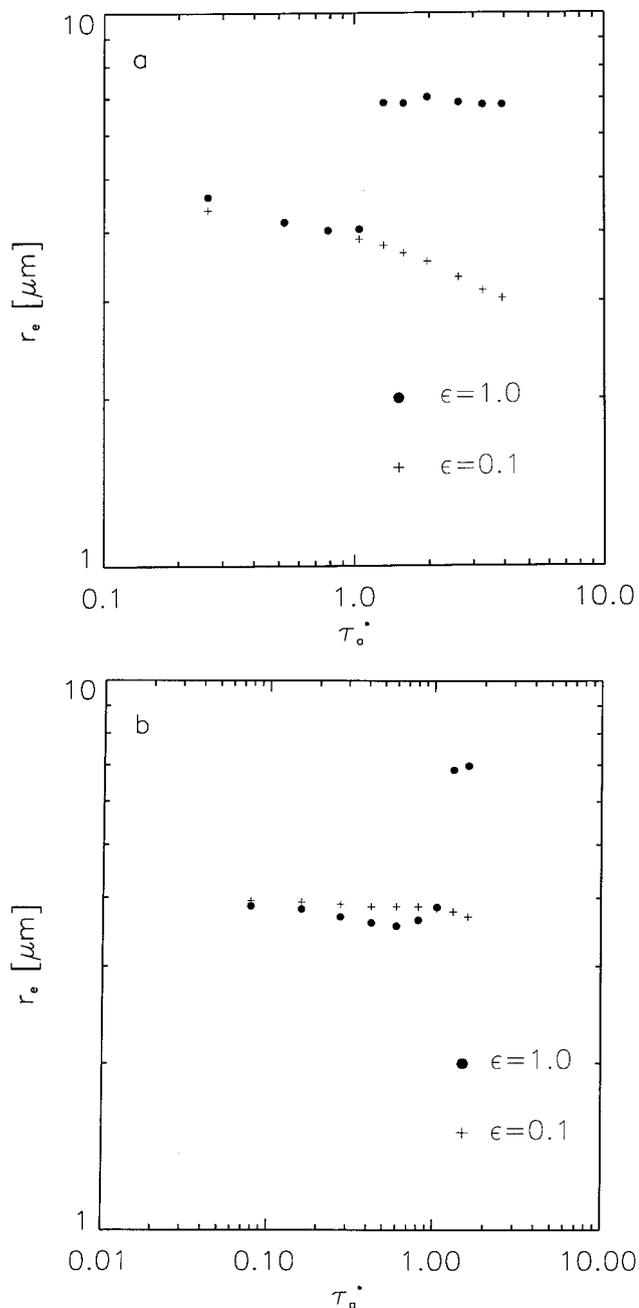


**Figure 7.** Model calculations of  $r_e$  for given  $\tau_a^*$ , where  $\tau_a^*$  is arbitrarily defined as  $\tau_a$  for a homogeneous smoke layer of 500 m depth. Calculations are for  $\sigma = 2$ , and  $w = 300 \text{ cm s}^{-1}$ . (a) for  $r_g = 0.1 \text{ }\mu\text{m}$  and variable  $N_a$ ; (b) for  $N_a = 10,000 \text{ cm}^{-3}$  and variable  $r_g$ . At large  $N_a$ , or  $r_g$ , the IE (slope of the curve) is negligible and may even be negative, especially for  $\epsilon = 1$ .

not unexpected. Again, we point to Twomey's [1959] solution (equation (12)) which shows that the dependence of  $N_d$  on aerosol concentration and  $w$  is dependent on the aerosol size distribution parameter  $k$ .

**4.1. Identification of Three Primary Responses**

On the basis of Plate 3 and Table 2, three primary responses of cloud microphysics to aerosol parameters and updraft are



**Figure 8.** As in Figure 7 but for calculations at  $\sigma = 2$  and  $w = 50 \text{ cm s}^{-1}$ : (a) for  $r_g = 0.11 \mu\text{m}$  and variable  $N_a$ ; (b) for  $N_a = 10,000 \text{ cm}^{-3}$  and variable  $r_g$ . For  $\epsilon = 1$ ,  $r_e$  increases at large  $N_a$ , or  $r_g$  implying a negative IE. This is related to competition for vapor resulting in the evaporation of droplets. For  $\epsilon = 0.1$ ,  $r_e$  is fairly constant with increasing  $N_a$  or  $r_g$  but tends to decrease more sharply at very large  $N_a$  or  $r_g$ .

identified. A conceptual plot of these three responses is given in Figure 6.

**4.1.1. (i) Cloud droplet concentrations increase with increasing aerosol loading, followed by saturation in the response at high concentrations.** When  $w$  is large, there is a tendency for IE to decrease with increasing  $N_a$  and  $r_g$  (Plate 3b). At large  $w$ , supersaturation production is adequate, and for low  $N_a$  and  $r_g$ , there is a strong correlation between  $N_d$  and smoke loading (large IE). However, as  $N_a$  and  $r_g$  increase,

competition for vapor hinders growth, fewer and fewer new particles can be activated, and IE becomes progressively smaller. (When  $N_a$  is very large, the competition for vapor among particles is enormous and the definition of what constitutes a drop, rather than a haze particle, is somewhat arbitrary. In our analysis we do not adhere to the strict definition of activation but assume that particles with radii greater than  $1 \mu\text{m}$  are activated drops, to facilitate comparison with in situ measurements of cloud droplets using forward light scattering probes (FSSP) (particle measuring systems). In some cases this may underestimate the number concentration of optically active haze particles/drops [see also Reid *et al.*, 1999].) This implies that  $N_d$  and  $r_e$  become progressively less dependent on  $\tau_a^*$ ; that is, they reach saturation. This result is consistent with observations from much cleaner conditions [e.g., Martin *et al.*, 1994], which indicate a saturation in  $N_d$  when  $N_a$  increases above some threshold.

**4.1.2. (ii) Cloud droplet concentrations increase with increasing aerosol loading, saturation in the response (as in i), followed by an increase in droplet concentrations.** When  $w$  is small, there are two regions of higher IE: one at small  $N_a$  and  $r_g$ , and a second at large  $N_a$  and  $r_g$ , with a minimum in between (Plate 3a). As in i, there is a strong correlation between  $N_d$  and aerosol loading at low  $N_a$  and  $r_g$  which results in higher IE. However, because at small  $w$  the system is limited by low supersaturation production, increases in  $N_a$  and  $r_g$  result in strong competition for available vapor and a more rapid decrease in IE. A close analysis of the model output shows that further increases in  $N_a$  and  $r_g$  create a situation where large particles suppress supersaturation at the early stages of activation [Ghan *et al.*, 1998; Feingold and Kreidenweis, 2000] and prevent many of the smaller particles from activating; these smaller particles are especially difficult to activate when  $\epsilon = 0.1$ . The absence of smaller drops, which are efficient at taking up water vapor, allows a slower but sustained activation of larger particles and results in larger IE. Note that if  $w$  were large enough, the largest particles would not be able to suppress activation of many of the smaller particles, which is why the secondary peak is not observed at the higher  $w$ . We are unaware of observational evidence for these two regions, but note that this implies that there may be potential for further activation after the system is saturated, i.e., beyond the point of IE = 0.

**4.1.3. (iii) Cloud droplet concentrations increase with aerosol loading, saturation in response (as in i), followed by a negative response as intense competition for vapor evaporates the smallest droplets.** When particles are very hydrophilic ( $\epsilon = 1$ ), activation is facilitated, and competition for vapor is so strong that after the response of the cloud to the addition of particles has saturated (IE  $\approx 0$ ), the addition of more particles results in a steady evaporation of smaller drops and negative IE. This indicates an unexpected increase in  $r_e$  (or decrease in  $N_d$ ) with increasing  $\tau_a^*$ . The largest negative values of IE occur at large  $N_a$  and large  $r_g$  (Plates 3c and 3d). Again, we know of no observational evidence for negative IE, but note that if it does occur in nature, it constitutes an interesting microphysical feedback; at very high aerosol loadings, competition for available water vapor may act to reverse the general tendency for drop number to increase with increasing aerosol concentration.

To examine this more closely, Figure 7 illustrates individual model calculations of  $r_e$  for given  $\tau_a^*$ , where  $\tau_a^*$  is arbitrarily defined as  $\tau_a^*$  for a homogeneous smoke layer of 500 m depth.

Calculations are performed at fixed  $\sigma = 2$ , and  $w = 300 \text{ cm s}^{-1}$ ; individual points pertain to the values of  $N_a$  (Figure 7a) and to the values of  $r_g$  (Figure 7b) in Table 1. In the case of  $\varepsilon = 0.1$ , the slope of  $\log r_e$  versus  $\log \tau_a$  decreases gradually with increasing  $\tau_a$  (or  $N_a$ ). For  $\varepsilon = 1.0$ , the slope tends to zero and then reverses to a positive slope, or negative IE. Figure 8 further exemplifies the negative IE response by examining an equivalent simulation at low  $w$ . The results for  $\varepsilon = 0.1$  in Figure 8 also capture the increase in IE at high  $\tau_a^*$ , which is indicated by response (ii).

The cases including entrainment (Plates 3e and 3f) illustrate a dependence of IE on  $N_a$  and  $r_g$  similar to ii with two maxima in IE. Entrainment of dry air enhances the effects outlined in ii by forcing the numerous small droplets to evaporate; larger drops are more robust to evaporation and may even grow at the expense of small drops. The highest modeled IE occur under these conditions when  $w$  is small. Table 2 supports this argument by showing that entrainment results in larger, and positive values of  $a_2$  and  $a_3$ ; that is, the model indicates that increases in  $r_g$  and  $\sigma$  will increase IE by supplying larger droplets that are more robust to the entrainment drying.

Plate 4 plots satellite-derived values of IE and places them in  $N_a, r_g$  parameter space as in Plate 3. Two different values of  $r_g$  have been assumed, and  $N_a$  has been derived from  $\tau_a$  assuming a fixed  $\sigma = 1.82$ . The derived values of  $N_a$  for assumed  $r_g$  depend primarily on  $\sigma$  and on the assumed depth of the smoke layer. If  $\sigma$  and/or the depth of the smoke layer were assumed smaller, the derived  $N_a$  would be larger, and vice versa; for this reason we do not attempt to match the same  $N_a, r_g$  values as in Plate 3 but concentrate rather on observed trends. In general, model-derived values of IE are consistent with the observed values. In the north the satellite-derived IE of 0.38 in 1995 is large and only exceeded by modeled values of IE in Plate 3e for conditions of low  $w$ , low solubility, and subadiabatic conditions. In 1987 there is a monotonic decrease in IE with increasing  $N_a$  (and  $\tau_a$ ) which is akin to the model results in Plate 3b. However, in 1995 the data points have larger IE at both lower and higher  $N_a$  (or  $\tau_a$ ), with a smaller value at the intermediate value of  $N_a$  (or  $\tau_a$ ). This follows the pattern for response ii (Plates 3a and 3e). We note that the 1995 burning season was characterized by an anomalously strong inversion [Nobre *et al.*, 1998], and if we assume that this resulted in weaker convection, comparison of the 1995 data with the weaker updrafts of Plates 3a and 3e is appropriate. The consistency between Plate 4b and response ii does support the idea that response ii actually occurs in real clouds, but clearly, more data would be required to place this hypothesis on firmer ground.

#### 4.2. Dependence of the Indirect Effect on $\tau_a$

The modeling results indicate that  $\tau_a$  is not necessarily a sufficient determinant of IE. This conclusion is arrived at by calculating IE for subsets of lognormal parameter space (Table 1), determining the  $\tau_a$  range given by these parameters, and then calculating IE on a new subset of the model output that encompasses the very same  $\tau_a$  range, but with no restrictions on the lognormal parameters. (See table entries labeled “equivalent  $\tau_a$ ” in Table 2.) The exercise determines to what extent  $\tau_a$  is a good proxy for the detailed size distribution information. For example, Table 2 indicates that a very weak indirect effect (IE = 0.08) is obtained when  $r_g > 0.08 \text{ }\mu\text{m}$ ,  $N_a > 5000 \text{ cm}^{-3}$ , and  $w \geq 200 \text{ cm s}^{-1}$ . If the model output is then resorted according to the  $\tau_a$  range prescribed by those

same parameters ( $r_g > 0.08 \text{ }\mu\text{m}$  and  $N_a > 5000 \text{ cm}^{-3}$ ), but this time with no restriction on the lognormal parameter space, a much more significant indirect response of IE = 0.19 is obtained. Similarly, when the IE has a significant value of 0.30 for  $r_g \leq 0.08 \text{ }\mu\text{m}$ ,  $N_a \leq 5000 \text{ cm}^{-3}$ , and  $w \leq 200 \text{ cm s}^{-1}$ , the “equivalent  $\tau_a$ ” yields a much reduced indirect effect (IE = 0.22). To first order  $\tau_a$  is probably a good measure of IE, but this analysis suggests that the details of the aerosol size distribution, even when parameterized with a simple lognormal function, may be important.

One should bear in mind that the parameter space for aerosol reflects the large number concentrations of particles found in smoke (up to 2 orders of magnitude greater than typical continental concentrations not prone to smoke) and that the present analysis may not be applicable to those typical scenarios. Similar analyses could easily be performed for much cleaner conditions than those examined here.

#### 4.3. Susceptibility

The tendency for the indirect effect to be strongest at the lowest smoke optical depths is analogous to the concept of susceptibility  $S$  introduced by Platnick and Twomey [1994]:

$$S = \left. \frac{d\rho}{dN_d} \right|_{\text{const LW}} = \frac{\rho(1-\rho)}{3N_d}, \quad (28)$$

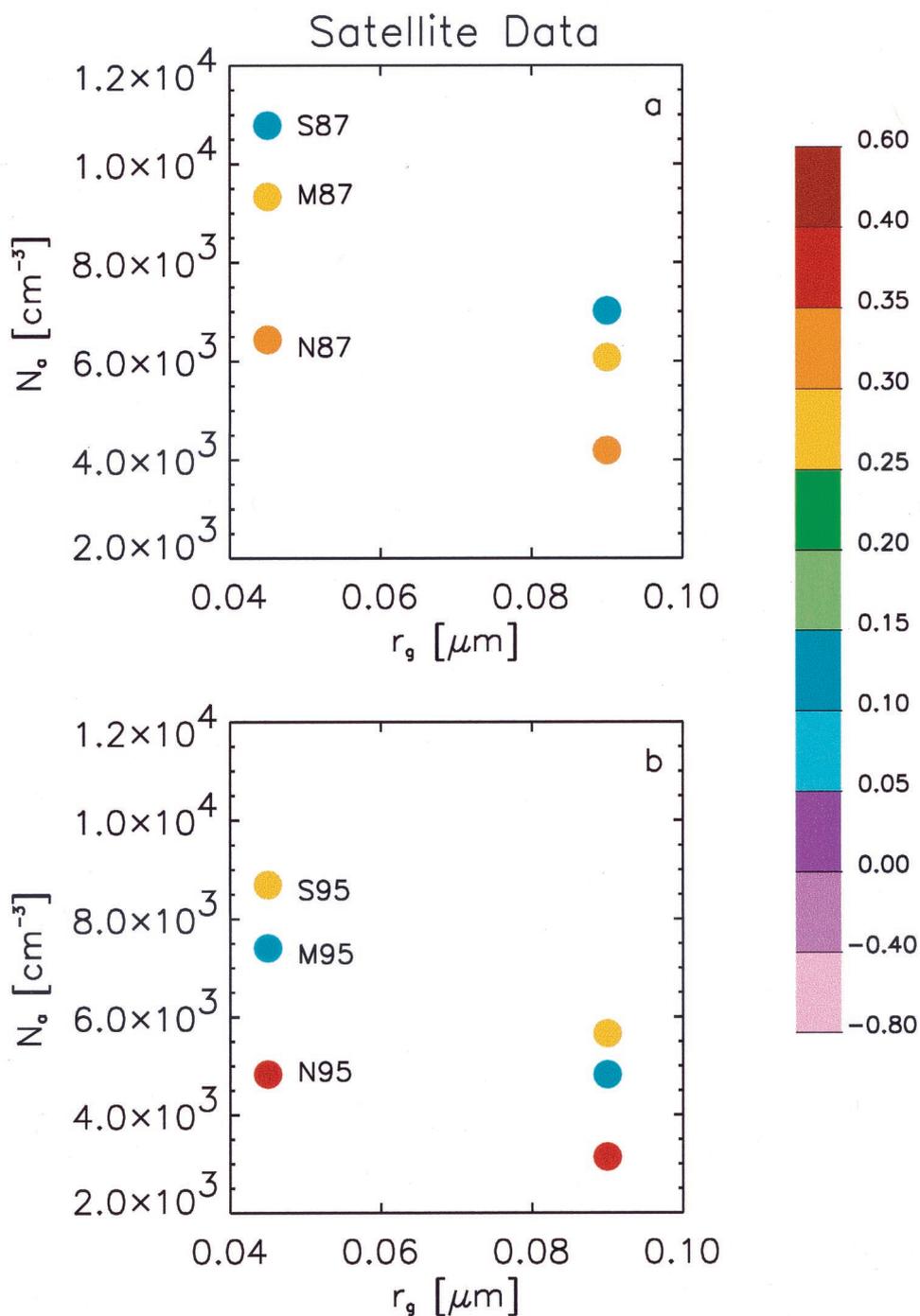
or simply,

$$\frac{d \ln \rho}{d \ln N_d} = \frac{(1-\rho)}{3}. \quad (29)$$

Equation (28) predicts that clouds forming in cleaner environments (larger drops, and lower  $\rho$ ) will have a stronger response to the addition of drops than equivalent, more reflective clouds. For a very reflective cloud with  $\rho = 1$ , the response is zero. There is a fundamental difference between  $S$ , as defined by (28), and IE, as defined by (2);  $S$  relies on a measure of  $N_d$ , while IE casts the change in cloud properties (in this case,  $r_e$ , or  $\rho$ , in the case of (23)) in terms of a bulk aerosol property ( $\tau_a$ ). Susceptibility thus short-circuits the complex interaction between cloud droplet formation and aerosol properties, while IE must include them directly. Once equations for  $N_d$  in terms of aerosol parameters have been established (equations (10) and (11)), calculation of  $S$  is straightforward.

### 5. Summary

Analysis of aerosol-cloud interaction, or the “aerosol indirect effect,” has been undertaken using extensive satellite remote sensing measurements in the biomass burning regions of Brazil. Retrievals of cloud drop radius, cloud reflectance, and smoke optical depth enable assessment of the effect of smoke aerosol on cloud microphysical and optical properties [Kaufman and Nakajima, 1993]. This is usually described as the change in drop radius as a function of the change in smoke optical depth. KF97 suggested that PWV might be an additional parameter determining the indirect effect. The current analysis of 2 years of data does not support this hypothesis. Analysis indicates that the cloud drop response to aerosol is greatest in the north of Brazil, where aerosol optical depth is smallest, and tends to decrease as one moves southward, and as aerosol optical depth increases. Saturation in this response occurs at an aerosol optical depth of 0.8 in 1987 and 0.4 in 1995.



**Plate 4.** Satellite-derived IE in  $N_a$ ,  $r_g$  space assuming two different values of  $r_g$ , and with  $N_a$  derived from the measurement of  $\tau_a$ , and an assumed aerosol distribution breadth. The circles are labeled according to year (1987 or 1995) as well as according to latitudinal band: N (North), M (Middle), and S (South). (a) for 1987 data, (b) for 1995 data.

An analytical/modeling approach has been taken to unify the descriptions of aerosol-cloud interaction and to assist in evaluation of the indirect effect. This new framework extends Twomey's [1974] representation to include the effects of aerosol size distribution parameters. It retains the basic assumptions of a homogeneous cloud and compares aerosol effects for clouds of similar liquid water content. As such, it should be seen as a tool to explore first-order effects of aerosol-cloud interaction. It does not include aerosol-radiative-dynamical

feedbacks. It does show that variability in the observed saturation in indirect effect may be related to both dynamics, as well as aerosol size distribution and composition.

It is suggested that for remote sensing applications the indirect effect is best defined as a relative change in cloud drop size for a relative change in smoke optical depth since this alleviates measurement biases. A numerical model is used to generate the coefficients that quantify aerosol-cloud interaction. The model's incomplete description of this interaction

means that the most appropriate use of the model is to explore the relative importance of various aerosol parameters in determining cloud properties.

The new theoretical analysis is applied to the data analysis, and its utility in helping describe cloud response to smoke aerosol is demonstrated. Three primary responses are identified (Figure 6); the conditions under which each of these responses are to be expected are described in the text: (i) cloud droplet concentrations increase with increasing aerosol loading, followed by saturation in the response at very high concentrations; (ii) cloud droplet concentrations increase with increasing aerosol loading, saturation in the response (as in i), followed by an increase in response when sufficient large particles exist to quench supersaturation during the early stages of activation and prevent activation of smaller particles [Ghan *et al.*, 1998; Feingold and Kreidenweis, 2000]; (iii) cloud droplet concentrations increase with aerosol loading, saturation in response (as in i), followed by a negative response as intense competition for vapor evaporates the smallest droplets. Thus we hypothesize that at very high mass loadings, the microphysical response to smoke may not be monotonic.

Despite the apparent relationship between optical depth and strength of the indirect effect in the satellite analysis, the modeling study points to a different conclusion. Because the activation process is so strongly dependent on the aerosol size distribution, hygroscopicity, and supersaturation production, the modeling study suggests that optical depth is not always an adequate surrogate for describing the strength of the indirect effect.

This analysis has also yielded a simple empirical equation describing the number of drops activated as a function of aerosol size distribution parameters (parameterized as a log-normal function) as well as vertical velocity (equation (11)). The coefficients that quantify droplet activation have been calculated using regression fits to the model output for a large range of parameter space. This equation could easily be applied as a drop activation algorithm in general circulation models [e.g., Ghan *et al.*, 1993, 1997], but we caution that better accuracy can be attained when the coefficients are calculated over smaller sections of parameter space.

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